

Bis(2,3-diaminopyridinium) succinate trihydrate

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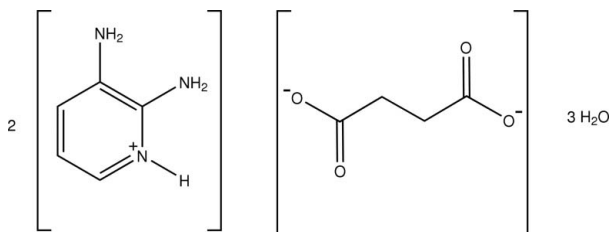
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Key indicators: single-crystal X-ray study; $T = 100$ K; mean $\sigma(\text{C}-\text{C}) = 0.003$ Å; disorder in main residue; R factor = 0.062; wR factor = 0.129; data-to-parameter ratio = 11.9.

In the title salt, $2\text{C}_5\text{H}_8\text{N}_3^+ \cdot \text{C}_4\text{H}_4\text{O}_4^{2-} \cdot 3\text{H}_2\text{O}$, the asymmetric unit contains a protonated 2,3-diaminopyridinium cation, half of a succinate dianion (disposed about a centre of inversion), and one and a half water molecules. One of the water molecules is disordered over two sites with occupancies of 0.670 (17) and 0.330 (17). The other water molecule has an occupancy of 0.5 (from refinement). The pyridine N atom of the 2,3-diaminopyridine molecule is protonated. The protonated N atom and one of the 2-amino H atoms are hydrogen bonded to the succinate anion through a pair of $\text{N}-\text{H} \cdots \text{O}$ hydrogen bonds, forming an $R_2^2(8)$ ring motif. In the crystal, molecules are consolidated into a three-dimensional network by $\text{N}-\text{H} \cdots \text{O}$ and $\text{O}-\text{H} \cdots \text{O}$ interactions.

Related literature

For substituted pyridines, see: Pozharski *et al.* (1997); Katritzky *et al.* (1996); Jeffrey & Saenger (1991); Jeffrey (1997); Scheiner (1997). For related structures, see: De Cires-Mejias *et al.* (2004); Fun & Balasubramani (2009); Balasubramani & Fun (2009a,b). For the stability of the temperature controller used in the data collection, see: Cosier & Glazer (1986). For hydrogen-bond motifs, see: Bernstein *et al.* (1995).



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[§] Thomson Reuters ResearcherID: A-5523-2009.

Experimental

Crystal data

$2\text{C}_5\text{H}_8\text{N}_3^+ \cdot \text{C}_4\text{H}_4\text{O}_4^{2-} \cdot 3\text{H}_2\text{O}$
 $M_r = 195.20$
 Monoclinic, $P2_1/c$
 $a = 12.7159$ (4) Å
 $b = 3.9024$ (1) Å
 $c = 18.7734$ (6) Å
 $\beta = 94.933$ (2)°

$V = 928.13$ (5) Å³
 $Z = 4$
 Mo $K\alpha$ radiation
 $\mu = 0.11$ mm⁻¹
 $T = 100$ K
 $0.17 \times 0.13 \times 0.06$ mm

Data collection

Bruker SMART APEXII CCD
 area-detector diffractometer
 Absorption correction: multi-scan
 (SADABS; Bruker, 2005)
 $T_{\min} = 0.981$, $T_{\max} = 0.993$

10934 measured reflections
 2121 independent reflections
 1364 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.056$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.062$
 $wR(F^2) = 0.129$
 $S = 1.06$
 2121 reflections
 178 parameters

H atoms treated by a mixture of independent and constrained refinement
 $\Delta\rho_{\text{max}} = 0.26$ e Å⁻³
 $\Delta\rho_{\text{min}} = -0.24$ e Å⁻³

Table 1

Hydrogen-bond geometry (Å, °).

$D-H \cdots A$	$D-H$	$H \cdots A$	$D \cdots A$	$D-H \cdots A$
$\text{N2}-\text{H2N2} \cdots \text{O1}^i$	0.90 (3)	2.14 (3)	2.978 (3)	155 (3)
$\text{N3}-\text{H1N3} \cdots \text{O1}^i$	0.85 (3)	2.14 (3)	2.993 (3)	176 (3)
$\text{N3}-\text{H2N3} \cdots \text{O1WA}^{ii}$	0.91 (3)	2.34 (3)	3.243 (6)	172 (2)
$\text{O1WA}-\text{H2WA} \cdots \text{O2}$	0.85	1.93	2.764 (5)	165
$\text{N2}-\text{H1N2} \cdots \text{O1}$	0.89 (3)	2.04 (3)	2.929 (3)	175 (2)
$\text{N1}-\text{H1N1} \cdots \text{O2}$	0.96 (3)	1.69 (3)	2.643 (3)	171 (2)

Symmetry codes: (i) $-x, y - \frac{1}{2}, -z + \frac{1}{2}$; (ii) $x, -y + \frac{1}{2}, z - \frac{1}{2}$.

Data collection: *APEX2* (Bruker, 2005); cell refinement: *SAINTE* (Bruker, 2005); data reduction: *SAINTE*; program(s) used to solve structure: *SHELXTL* (Sheldrick, 2008); program(s) used to refine structure: *SHELXTL*; molecular graphics: *SHELXTL*; software used to prepare material for publication: *SHELXTL* and *PLATON* (Spek, 2009).

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: TK2489).

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supplementary materials

Acta Cryst. (2009). E65, o1854-o1855 [doi:10.1107/S1600536809026439]

Bis(2,3-diaminopyridinium) succinate trihydrate

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Comment

Pyridine and its derivatives play an important role in heterocyclic chemistry (Pozharski *et al.*, 1997; Katritzky *et al.*, 1996). Further, pyridine and its substituted derivatives are often involved in hydrogen-bond interactions (Jeffrey & Saenger, 1991; Jeffrey, 1997; Scheiner, 1997). The crystal structures of 2,3-diaminopyridinium 4-hydroxybenzoate (Fun & Balasubramani, 2009), 2,3-diaminopyridinium 4-nitrobenzoate (Balasubramani & Fun, 2009a) and 2,3-diaminopyridinium benzoate (Balasubramani & Fun, 2009b) have been reported by us recently. In the hope to study some interesting hydrogen-bonding interactions, the title compound (I) was synthesized. Its molecular and crystal structure is presented here.

The asymmetric unit of (I) (Fig. 1), contains a protonated 2,3-diaminopyridinium cation, a half molecule of succinate anion (disposed about a centre of inversion), and one and half water molecules. In the 2,3-diaminopyridinium cation, protonation N1 atom has lead to a slight increase (ca. 4 °) in the C1—N1—C5 angle to 123.6 (2)° compared with the unprotonated structure (De Cires-Mejias *et al.*, 2004). The 2,3-diaminopyridinium cation is planar, with a maximum deviation of 0.004 (2) Å for atom C2.

In the crystal packing (Fig. 2), the protonated N1 atom and a nitrogen atom of the 2-amino group (N2) are hydrogen-bonded to the succinate oxygen atoms (O2 and O1) *via* a pair of N—H···O hydrogen bonds forming a ring motif $R_2^2(8)$ (Bernstein *et al.*, 1995). The 2-amino groups (N2 and N3) are involved in N—H···O hydrogen-bonding interactions to form a $R_2^1(7)$ ring motif. The crystal structure is further stabilized by water molecules *via* O(water)—H···O and N—H···O(water) hydrogen bonding (Table 1 and Fig. 2).

Experimental

An aqueous solution of hot methanol (10 ml/ 10 ml) of 2,3-diaminopyridine (27 mg, Aldrich) and succinic acid (29 mg, Merck) were mixed and warmed over a heating magnetic stirrer for 5 minutes. The resulting solution was allowed to cool slowly at room temperature. Crystals of (I) appeared from the mother liquor after a few days.

Refinement

All the H atoms (other than the water H-atoms) were located from the difference Fourier map and allowed to refine freely [N—H = 0.85 (3)–0.96 (3) Å & C—H = 0.93 (2)–0.98 (2) Å]. The water H-atoms were located from the difference Fourier map but constrained to 0.85 Å from the parent atom with $U_{\text{iso}}(\text{H}) = 1.5U_{\text{eq}}(\text{O})$.

One water molecule has a refined occupancy of 0.495 (7) which was then fixed as 0.5 in the final refinement. The other water molecule is disordered (O1WA & O1WB) over two sites with occupancies of 0.670 (17) and 0.330 (17).

Figures

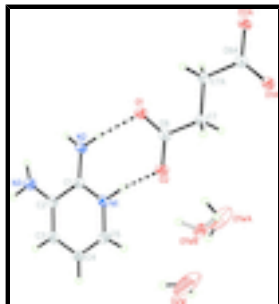


Fig. 1. The molecular structure of (I), showing 50% probability displacement ellipsoids and the atom numbering scheme. Dashed lines indicate the hydrogen bonding. The O1 water molecule is disordered over two positions. Symmetry operation A: $-x, 2-y, 1-z$.

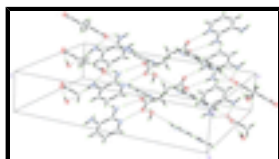


Fig. 2. Part of the crystal packing showing the overall 3-D hydrogen-bonding network in (I). Dashed lines indicate the hydrogen bonding.

Bis(2,3-diaminopyridinium) succinate trihydrate

Crystal data



$M_r = 195.20$

Monoclinic, $P2_1/c$

Hall symbol: $-P\ 2ybc$

$a = 12.7159\ (4)\ \text{\AA}$

$b = 3.90240\ (10)\ \text{\AA}$

$c = 18.7734\ (6)\ \text{\AA}$

$\beta = 94.933\ (2)^\circ$

$V = 928.13\ (5)\ \text{\AA}^3$

$Z = 4$

$F_{000} = 416$

$D_x = 1.397\ \text{Mg m}^{-3}$

Mo $K\alpha$ radiation, $\lambda = 0.71073\ \text{\AA}$

Cell parameters from 2108 reflections

$\theta = 2.2\text{--}30.0^\circ$

$\mu = 0.11\ \text{mm}^{-1}$

$T = 100\ \text{K}$

Block, brown

$0.17 \times 0.13 \times 0.06\ \text{mm}$

Data collection

Bruker SMART APEXII CCD area-detector diffractometer

Radiation source: fine-focus sealed tube

Monochromator: graphite

$T = 100\ \text{K}$

φ and ω scans

Absorption correction: multi-scan (SADABS; Bruker, 2005)

$T_{\min} = 0.981, T_{\max} = 0.993$

10934 measured reflections

2121 independent reflections

1364 reflections with $I > 2\sigma(I)$

$R_{\text{int}} = 0.056$

$\theta_{\max} = 27.5^\circ$

$\theta_{\min} = 2.6^\circ$

$h = -16 \rightarrow 16$

$k = -4 \rightarrow 5$

$l = -24 \rightarrow 21$

Refinement

Refinement on F^2	Secondary atom site location: difference Fourier map
Least-squares matrix: full	Hydrogen site location: inferred from neighbouring sites
$R[F^2 > 2\sigma(F^2)] = 0.062$	H atoms treated by a mixture of independent and constrained refinement
$wR(F^2) = 0.129$	$w = 1/[\sigma^2(F_o^2) + (0.041P)^2 + 0.7373P]$
$S = 1.06$	where $P = (F_o^2 + 2F_c^2)/3$
2121 reflections	$(\Delta/\sigma)_{\max} < 0.001$
178 parameters	$\Delta\rho_{\max} = 0.26 \text{ e } \text{\AA}^{-3}$
Primary atom site location: structure-invariant direct methods	$\Delta\rho_{\min} = -0.24 \text{ e } \text{\AA}^{-3}$
	Extinction correction: none

Special details

Experimental. The crystal was placed in the cold stream of an Oxford Cryosystems Cobra open-flow nitrogen cryostat (Cosier & Glazer, 1986) operating at 100.0 (1) K.

Geometry. All s.u.'s (except the s.u. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell s.u.'s are taken into account individually in the estimation of s.u.'s in distances, angles and torsion angles; correlations between s.u.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell s.u.'s is used for estimating s.u.'s involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R-factor wR and goodness of fit S are based on F^2 , conventional R-factors R are based on F , with F set to zero for negative F^2 . The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R-factors(gt) etc. and is not relevant to the choice of reflections for refinement. R-factors based on F^2 are statistically about twice as large as those based on F , and R-factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$	Occ. (<1)
O1	0.02464 (12)	0.7567 (4)	0.37851 (8)	0.0251 (4)	
O2	0.18198 (12)	0.6548 (5)	0.43615 (8)	0.0264 (4)	
N1	0.25383 (14)	0.2963 (5)	0.33114 (10)	0.0204 (5)	
N2	0.10876 (15)	0.4334 (6)	0.25459 (12)	0.0243 (5)	
N3	0.20743 (19)	0.1167 (7)	0.14153 (12)	0.0328 (6)	
C1	0.20422 (17)	0.2863 (6)	0.26523 (12)	0.0201 (5)	
C2	0.25526 (17)	0.1188 (6)	0.20981 (12)	0.0221 (6)	
C3	0.35320 (18)	-0.0256 (7)	0.22796 (13)	0.0243 (6)	
C4	0.40151 (18)	-0.0059 (7)	0.29740 (13)	0.0248 (6)	
C5	0.35068 (18)	0.1562 (7)	0.34840 (13)	0.0241 (6)	
C6	0.08824 (17)	0.7727 (6)	0.43321 (12)	0.0207 (5)	
C7	0.05630 (18)	0.9358 (7)	0.50147 (12)	0.0207 (5)	
O1WA	0.3424 (4)	0.840 (3)	0.5375 (3)	0.082 (3)	0.670 (17)
H1WA	0.3803	0.6625	0.5341	0.123*	0.670 (17)
H2WA	0.2898	0.8222	0.5066	0.123*	0.670 (17)

supplementary materials

O1WB	0.3443 (6)	0.583 (4)	0.5327 (3)	0.039 (4)	0.330 (17)
H1WB	0.3312	0.7954	0.5365	0.058*	0.330 (17)
H2WB	0.3173	0.5182	0.4919	0.058*	0.330 (17)
O2W	0.4593 (3)	0.248 (2)	0.5467 (3)	0.110 (3)	0.50
H1W2	0.5119	0.3543	0.5322	0.165*	0.50
H2W2	0.4462	0.0794	0.5187	0.165*	0.50
H4A	0.4676 (19)	-0.100 (7)	0.3090 (12)	0.027 (7)*	
H5A	0.3781 (17)	0.185 (6)	0.3960 (13)	0.022 (6)*	
H3A	0.3854 (18)	-0.140 (7)	0.1902 (13)	0.030 (7)*	
H7B	0.0722 (17)	0.759 (6)	0.5381 (12)	0.020 (6)*	
H7A	0.1062 (18)	1.118 (7)	0.5145 (12)	0.026 (7)*	
H2N2	0.076 (2)	0.445 (8)	0.2102 (16)	0.047 (9)*	
H1N3	0.142 (2)	0.154 (7)	0.1337 (14)	0.037 (8)*	
H1N2	0.0799 (19)	0.537 (7)	0.2905 (14)	0.028 (7)*	
H2N3	0.239 (2)	-0.022 (8)	0.1105 (15)	0.045 (9)*	
H1N1	0.2213 (19)	0.418 (7)	0.3676 (13)	0.030 (7)*	

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
O1	0.0211 (8)	0.0345 (11)	0.0203 (8)	0.0028 (8)	0.0054 (7)	-0.0005 (7)
O2	0.0188 (8)	0.0361 (11)	0.0253 (9)	0.0030 (8)	0.0074 (7)	-0.0010 (8)
N1	0.0177 (10)	0.0213 (12)	0.0235 (10)	-0.0029 (9)	0.0084 (8)	-0.0007 (9)
N2	0.0203 (11)	0.0296 (13)	0.0239 (11)	0.0020 (10)	0.0066 (9)	-0.0041 (10)
N3	0.0263 (13)	0.0450 (16)	0.0277 (12)	0.0052 (12)	0.0056 (10)	-0.0071 (11)
C1	0.0172 (11)	0.0179 (13)	0.0259 (12)	-0.0052 (10)	0.0067 (9)	0.0016 (10)
C2	0.0219 (12)	0.0213 (14)	0.0242 (12)	-0.0050 (11)	0.0074 (10)	-0.0006 (10)
C3	0.0229 (12)	0.0215 (15)	0.0304 (13)	-0.0033 (11)	0.0134 (10)	-0.0025 (11)
C4	0.0153 (12)	0.0234 (14)	0.0366 (14)	-0.0026 (11)	0.0067 (10)	0.0008 (12)
C5	0.0204 (12)	0.0251 (15)	0.0269 (13)	-0.0031 (11)	0.0028 (10)	0.0024 (11)
C6	0.0219 (12)	0.0185 (14)	0.0229 (12)	-0.0022 (11)	0.0082 (10)	0.0049 (10)
C7	0.0207 (12)	0.0212 (14)	0.0204 (12)	-0.0003 (11)	0.0035 (10)	0.0027 (11)
O1WA	0.068 (3)	0.111 (8)	0.061 (3)	-0.030 (3)	-0.026 (2)	0.022 (3)
O1WB	0.031 (4)	0.064 (9)	0.020 (3)	0.009 (4)	-0.002 (2)	-0.009 (3)
O2W	0.039 (3)	0.210 (8)	0.078 (4)	-0.015 (4)	-0.016 (3)	-0.006 (4)

Geometric parameters (\AA , $^\circ$)

O1—C6	1.253 (3)	C4—H4A	0.93 (2)
O2—C6	1.274 (3)	C5—H5A	0.94 (2)
N1—C1	1.340 (3)	C6—C7	1.517 (3)
N1—C5	1.361 (3)	C7—C7 ⁱ	1.513 (4)
N1—H1N1	0.96 (3)	C7—H7B	0.98 (2)
N2—C1	1.342 (3)	C7—H7A	0.97 (3)
N2—H2N2	0.90 (3)	O1WA—H1WA	0.8500
N2—H1N2	0.89 (3)	O1WA—H2WA	0.8501
N3—C2	1.371 (3)	O1WA—H1WB	0.2257
N3—H1N3	0.85 (3)	O1WB—H1WA	0.5518

N3—H2N3	0.91 (3)	O1WB—H2WA	1.2381
C1—C2	1.431 (3)	O1WB—H1WB	0.8500
C2—C3	1.383 (3)	O1WB—H2WB	0.8502
C3—C4	1.395 (3)	O2W—H1W2	0.8500
C3—H3A	0.96 (3)	O2W—H2W2	0.8501
C4—C5	1.357 (3)		
C1—N1—C5	123.6 (2)	C4—C5—H5A	124.5 (14)
C1—N1—H1N1	118.5 (14)	N1—C5—H5A	115.7 (14)
C5—N1—H1N1	117.9 (14)	O1—C6—O2	123.6 (2)
C1—N2—H2N2	120.3 (18)	O1—C6—C7	120.8 (2)
C1—N2—H1N2	120.5 (15)	O2—C6—C7	115.61 (19)
H2N2—N2—H1N2	119 (2)	C7 ⁱ —C7—C6	115.4 (2)
C2—N3—H1N3	120.8 (18)	C7 ⁱ —C7—H7B	113.3 (13)
C2—N3—H2N3	114.7 (17)	C6—C7—H7B	104.0 (13)
H1N3—N3—H2N3	118 (3)	C7 ⁱ —C7—H7A	111.3 (14)
N1—C1—N2	118.2 (2)	C6—C7—H7A	107.7 (14)
N1—C1—C2	118.5 (2)	H7B—C7—H7A	104.4 (18)
N2—C1—C2	123.2 (2)	H1WA—O1WA—H2WA	107.4
N3—C2—C3	123.1 (2)	H1WA—O1WA—H1WB	73.7
N3—C2—C1	119.4 (2)	H2WA—O1WA—H1WB	54.6
C3—C2—C1	117.5 (2)	H1WA—O1WB—H2WA	91.7
C2—C3—C4	121.5 (2)	H1WA—O1WB—H1WB	67.4
C2—C3—H3A	116.1 (14)	H2WA—O1WB—H1WB	35.9
C4—C3—H3A	122.3 (14)	H1WA—O1WB—H2WB	118.6
C5—C4—C3	119.1 (2)	H2WA—O1WB—H2WB	72.5
C5—C4—H4A	119.8 (15)	H1WB—O1WB—H2WB	107.4
C3—C4—H4A	121.1 (15)	H1W2—O2W—H2W2	107.4
C4—C5—N1	119.7 (2)		
C5—N1—C1—N2	180.0 (2)	C1—C2—C3—C4	-0.8 (4)
C5—N1—C1—C2	0.2 (3)	C2—C3—C4—C5	0.6 (4)
N1—C1—C2—N3	-177.7 (2)	C3—C4—C5—N1	0.0 (4)
N2—C1—C2—N3	2.6 (4)	C1—N1—C5—C4	-0.4 (4)
N1—C1—C2—C3	0.4 (3)	O1—C6—C7—C7 ⁱ	1.6 (4)
N2—C1—C2—C3	-179.4 (2)	O2—C6—C7—C7 ⁱ	-177.9 (3)
N3—C2—C3—C4	177.2 (2)		

Symmetry codes: (i) $-x, -y+2, -z+1$.

Hydrogen-bond geometry ($\text{\AA}, ^\circ$)

$D-H\cdots A$	$D-H$	$H\cdots A$	$D\cdots A$	$D-H\cdots A$
N2—H2N2 \cdots O1 ⁱⁱ	0.90 (3)	2.14 (3)	2.978 (3)	155 (3)
N3—H1N3 \cdots O1 ⁱⁱ	0.85 (3)	2.14 (3)	2.993 (3)	176 (3)
N3—H2N3 \cdots O1WA ⁱⁱⁱ	0.91 (3)	2.34 (3)	3.243 (6)	172 (2)
O1WA—H2WA \cdots O2	0.85	1.93	2.764 (5)	165
N2—H1N2 \cdots O1	0.89 (3)	2.04 (3)	2.929 (3)	175 (2)
N1—H1N1 \cdots O2	0.96 (3)	1.69 (3)	2.643 (3)	171 (2)

Symmetry codes: (ii) $-x, y-1/2, -z+1/2$; (iii) $x, -y+1/2, z-1/2$.

Fig. 1

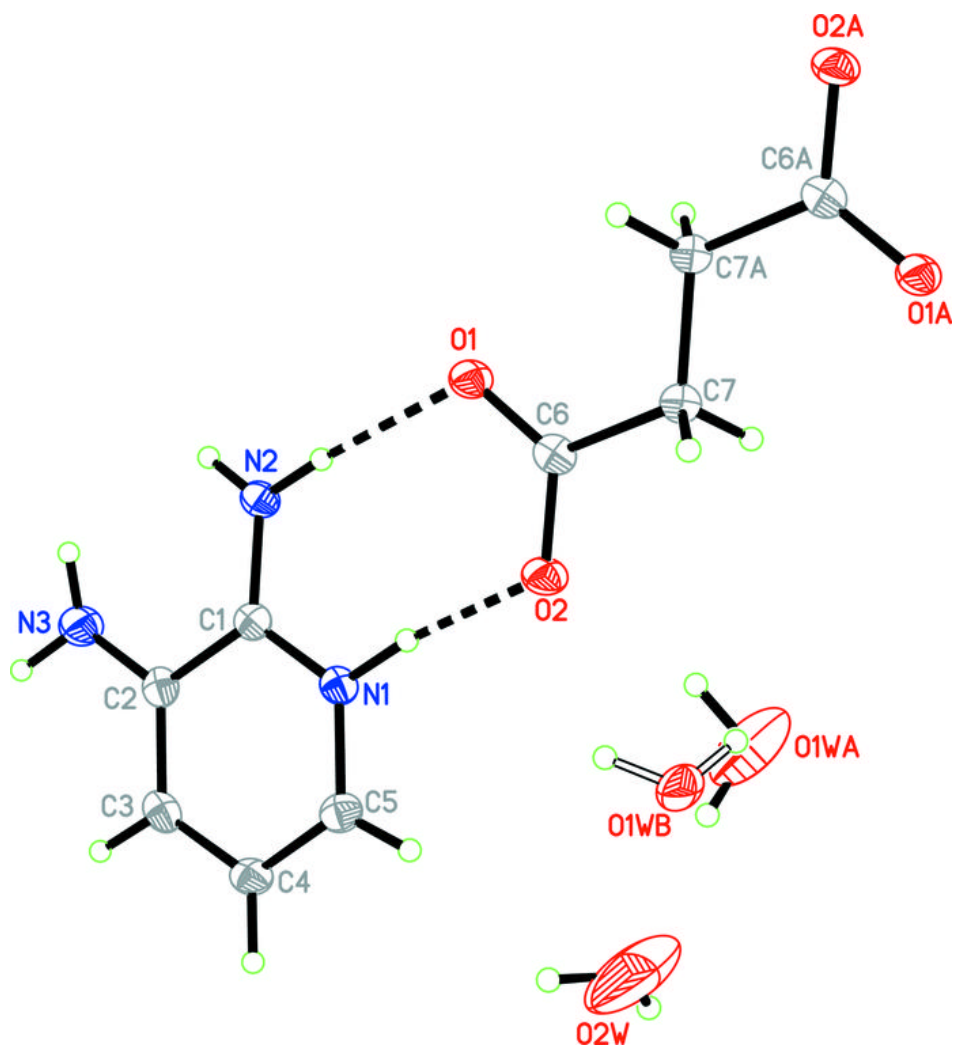


Fig. 2

